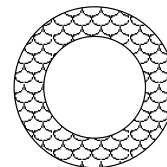


13. $8^{-2/3} = (?)$
 (A) -4 (B) $-\frac{16}{3}$ (C) $\frac{1}{8}$ (D) $\frac{3}{16}$ (E) $\frac{1}{4}$
14. $\tan^{-1}\left(\frac{4}{3}\right) - \tan^{-1}\left(\frac{1}{7}\right) = (?)$
 (A) $\frac{\pi}{6}$ (B) $\frac{\pi}{4}$ (C) $\frac{\pi}{2}$ (D) $\frac{\pi}{3}$ (E) 1
15. If $f(x) = x^2 - 2$, $f(x + 2) = (?)$
 (A) x^2 (B) $x^2 + 2$ (C) $x^2 + 4x + 2$
 (D) $x^3 - 4$ (E) $x^3 + 2x^2 - 2x - 4$
16. Find the solution of $\sec x - 1 = \tan x$ with $x \in [0, 2\pi)$.
 (A) 0 (B) $\frac{\pi}{2}$ (C) π (D) $\frac{4\pi}{3}$ (E) $\frac{3\pi}{2}$
17. What is the sum of the *squares* of the real and complex solutions of $x^4 + x^3 + 4x^2 + 4x = 0$?
 (A) -7 (B) -3 (C) 0 (D) 1 (E) 9
18. How many integers satisfy the inequality $|x^2 - 8| < 4$?
 (A) 0 (B) 1 (C) 2 (D) 3 (E) 4
19. Triangle ABC is inscribed in a circle with radius r . If $AB = r$, then $m\angle ACB = (?)$
 (A) 15° (B) 30° (C) 45° (D) 60° (E) 90°
20. $\frac{\sin 2x}{\sin x} = (?)$
 (A) 2 (B) $\sin 2$ (C) $\sec x$ (D) $\cos x$ (E) $2\cos x$
21. A circle has radius of length 5, is tangent to the line with equation $4x - 3y = 18$ at the point $(3, -2)$, and lies above the line. What is the equation of the circle?
 (A) $x^2 - 14x + y^2 + 10y = -49$
 (B) $x^2 - 6x + y^2 + 4y = 12$
 (C) $x^2 + 2x + y^2 - 2y = 3$
 (D) $x^2 + 2x + y^2 - 2y = 23$
 (E) $x^2 + 6x + y^2 + 4y = 12$
22. $32^{-(\sqrt{5})^{-2}} = (?)$
 (A) 32^6 (B) $\sqrt[3]{32}$ (C) 4 (D) $32^{2\sqrt{3}}$ (E) $\frac{1}{2}$
23. Find an equation of the perpendicular bisector of the segment connecting $A(-2, 3)$ and $B(6, -5)$.
 (A) $x + y = -1$ (B) $x - y = -1$ (C) $x - y = 3$
 (D) $x + 2y = -4$ (E) $2x + y = 2$

24. Three circles, each with radius of length 6, intersect so that each circle passes through the centers of the other two circles. Find the area of the region that is the intersection of the interiors of the three circles.

(A) $9\sqrt{3}$ (B) 6π (C) 9π
 (D) $18(\pi - \sqrt{3})$ (E) $48\pi - \sqrt{3}$

25. The diagram shows a circular pool surrounded by a garden of uniform width. The area of the garden is the same as the area of the surface of the pool. What is the ratio of the length of fencing needed to surround the pool to the length of fencing needed to enclose the entire region?

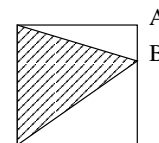


(A) $\frac{1}{4}$ (B) $\frac{\sqrt{2}}{4}$ (C) $\frac{1}{2}$ (D) $\frac{\sqrt{3}}{3}$ (E) $\frac{\sqrt{2}}{2}$

26. An investment with annual interest rate r yields an annual simple interest of \$1500. If \$500 more is invested and the rate is 2 percentage points less, the annual simple interest is \$1300. Find r .

(A) 7% (B) 8% (C) 9% (D) 11% (E) 12%

27. The diagram shows a square with sides of length 4. If $AB = x$, what is the ratio of the area of the shaded region to the total area of the unshaded regions?



(A) 1 (B) $\frac{1}{2}$ (C) $\frac{4}{x}$ (D) $2x$ (E) $\frac{4+x}{4-x}$

28. The areas of two similar hexagons are 150 square units and 200 square units. What is the ratio of the smaller perimeter to the larger perimeter?

(A) $\frac{\sqrt{2}}{3}$ (B) $\frac{\sqrt{2}}{2}$ (C) $\frac{\sqrt{3}}{3}$ (D) $\frac{\sqrt{3}}{2}$ (E) $\frac{\sqrt{6}}{5}$

29. Two distinct circles of radius 1 are tangent to each other. How many circles of radius 2 are tangent to both of them?

(A) 2 (B) 3 (C) 4 (D) 5 (E) 6

30. Find the final digit of $9^{412} \cdot 16^8$.

(A) 1 (B) 4 (C) 6 (D) 8 (E) 9

31. Solve for x : $|x - 1| < 3$

(A) $x < 2$ (B) $x < 4$ (C) $-2 < x < 4$
 (D) $x < -2$ or $x < 4$ (E) $x < -2$ or $x > 4$

32. The lengths of the sides of a triangle are $x + 5$, $2x - 1$, and 4. For how many values of x will the triangle be isosceles?

(A) 1 (B) 2 (C) 3 (D) 4 (E) 5

33. Where defined, $\frac{4}{x^2 + 6x + 8} - \frac{2}{x^2 + 7x + 12} = (?)$
- (A) $-\frac{2}{x + 4}$ (B) $\frac{2}{2x^2 + 13x + 20}$ (C) $\frac{2}{(x + 2)(x + 3)}$
(D) $\frac{2x + 5}{(x + 2)(x + 3)(x + 4)}$ (E) $\frac{2(x + 8)}{(x + 2)(x + 3)(x + 4)}$
34. The length of rectangle $ABCD$ is twice its width w . P is a point such that the area of $\triangle PBD$ is equal to the area of the rectangle. What is the length of the altitude of $\triangle PBD$ to the base BD ?
- (A) $\frac{w}{2}$ (B) $\frac{2w\sqrt{5}}{5}$ (C) $\frac{2w\sqrt{3}}{3}$ (D) $\frac{4w\sqrt{5}}{5}$ (E) $\frac{4w\sqrt{3}}{3}$
35. What is the product of the solutions to the equation $ax^2 + bx + c = 0$, where $a \neq 0$?
- (A) $4ac$ (B) $\frac{c}{2a}$ (C) $\frac{c}{a}$ (D) $\frac{b^2 - 2ac}{a}$ (E) $\frac{b^2 + 2ac}{a}$
36. In $\triangle ABC$, $AB = AC$ and $m\angle ABC \leq 60^\circ$. Which of the following is true?
- (A) BC must be greater than or equal to the lengths of the other sides of $\triangle ABC$.
(B) BC must be less than or equal to the lengths of the other sides of $\triangle ABC$.
(C) $\triangle ABC$ must be equilateral.
(D) $\angle BAC$ must be acute.
(E) $\angle BAC$ must be obtuse.
37. How many solutions are there to the equation $t^2 = |3t - 2|$?
- (A) 0 (B) 1 (C) 2 (D) 3 (E) 4
38. If ℓ , m , and n are distinct coplanar lines such that $\ell \perp n$ and $n \perp m$, which of the following is true?
- (A) $\ell \parallel n$
(B) $\ell \parallel m$
(C) $m \parallel n$
(D) $\ell \perp m$
(E) More information is needed to draw a conclusion.
39. Rationalize the denominator and simplify: $\frac{2\sqrt{6} + \sqrt{3}}{\sqrt{6} - \sqrt{3}} = (?)$
- (A) $1 + \sqrt{2}$ (B) $3 + 6\sqrt{2}$ (C) $4 + \sqrt{2}$ (D) $5 + 2\sqrt{2}$ (E) $5 + 3\sqrt{2}$
40. A person has a hours at his disposal. How many miles may he ride in a car traveling b miles per hour and yet have time to return on foot walking c miles per hour?
- (A) $\frac{ab^2}{a + b}$ (B) $\frac{ab - ac}{ab + c}$ (C) $\frac{abc}{b + c}$ (D) $\frac{ac}{b + c}$ (E) $\frac{b + c}{ac}$
41. \overleftrightarrow{CA} is tangent to a circle at A . \overleftrightarrow{CB} is tangent to the same circle at B . If $m\widehat{AB} = 100^\circ$, then $m\angle ACB = (?)$
- (A) 50° (B) 60° (C) 70° (D) 80° (E) 90°

